



## UG TRB Mathematics Syllabus

### UNIT-1 ALGEBRA and TRIGONOMETRY

Polynomial Equations – Imaginary and Irrational Roots – Relation between Roots and Coefficients symmetric function of Roots in terms of coefficient- Transformation of equation – Reciprocal equation - Increase or Decrease the roots of given equation – Removal of terms – Descartes's rule of signs – Approximate solution of roots of polynomial by Horner's Method–Cardan's method of solution of cubic polynomials – Summation of series using Binomial – Exponential and Logarithmic series. Symmetric – Skew symmetric, Hermitian – Skew Hermitian, Orthogonal Matrices, Unitary Matrices – Eigen Values – Eigen Vectors – Cayley-Hamilton Theorem – Similar Matrices – Diagonalization of Matrices. Prime Number, Composite Number, Decomposition of a Composite Number as a Product of primes uniquely – Divisor of a positive Integer – Euler Function. Congruence Modulo n, Highest power of prime number p Contained in  $n!$  – Application of Maxima and Minima – Prime and Composite numbers – Euler's function ( $\tilde{N}$ ) – Congruences – Fermat's, Wilson's and Lagrange's theorems. Expansions of Power of  $\sin nx$ ,  $\cos nx$ ,  $\tan nx$  – Summation by C + i S method, Telescopic Summation - Expansion of  $\sin x$ ,  $\cos x$ ,  $\tan x$  in terms of  $x$  - Sum of Roots of Trigonometric Equation, Formation of Equation With Trigonometric Roots - Hyperbolic Functions – Relation Between Circular and Hyperbolic Function – Inverse Hyperbolic Function – Logarithm of a complex number – Principal Value and General Values.

### UNIT II DIFFERENTIAL CALCULUS, INTEGRAL CALCULUS and ANALYTICAL GEOMETRY

$n$ th derivatives –Trigonometrical Transformations — Leibnitz Theorem – Implicit functions – Partial Differentiation – Maxima / Minima of a function of two variables – Lagrangian multiplier method - Radius of curvature in Cartesian and



Polar forms – Angle between radius vector and tangent – Slope of tangent of a polar curve –  $p-r$  equations – Center of  
Curvature – Evolutes, Envelopes – Asymptotes of Algebraic curves - Asymptotes by inspection –  
Intersection of a curve  
with asymptotes.  
Evaluation of Double and Triple integrals – Applications of Multiple Integrals in finding volumes,  
surface areas of  
solids – Areas of curved surfaces – Jacobians – Transformation of Integrals using Jacobians –  
Indefinite integrals - Beta  
and Gamma Functions and their properties – Evaluation of Integrals using Beta and Gamma  
Functions.  
Pole and Polar – Conjugate points and Conjugate lines, Conjugate diameters - Polar  
Coordinates – General Polar  
Equation of a Straight line – General Polar Equation of a Conic

## **UNIT-III DIFFERENTIAL EQUATIONS and LAPLACE TRANSFORMATIONS**

Ordinary Differential Equations - Homogeneous Equations - Exact equations - Integrating  
Factors - Linear  
equations - Reduction of order – Second order Linear differential equations – General solution  
of homogeneous  
Equations – Homogeneous equation with constant coefficients – Method of undetermined  
coefficients – method of  
Variation of Parameters - System of first order equations – Linear systems - Homogeneous  
linear systems with constant  
coefficients.  
Partial Differential Differential Equations - Formation of Partial Differential Differential Equations  
by eliminating  
arbitrary constants and arbitrary functions. Solving PDEs: Complete integral - Singular integral -  
general integral -  
Lagrange's equation  $Pp+Qq=R$  - Charpit's method and special types of first order equations.  
Laplace transform of elementary functions – Laplace transforms of special functions like unit  
step function. Dirac  
Delta function – Properties of Laplace Transformation and Laplace Transforms of derivatives  
and integrals – Evaluation  
of integrals using Laplace transform - Initial value theorem - Final value theorem – Laplace  
transform of periodic  
functions – Inverse Laplace transforms – Convolution theorem – Application of Laplace  
transformations in solving first



and second order linear differential equations and simultaneous linear ordinary differential equations.

## **UNIT –IV VECTOR CALCULUS and FOURIER SERIES, FOURIER TRANSFORMS**

Vector Differentiation – Velocity and Acceleration – Vector valued functions and Scalar potentials – Gradient –  
Divergence – Curl – Directional Derivative – Unit normal to a surface – Laplacian double operator – Harmonic functions.  
Vector Integration – Line Integral – Conservative force field – Determining Scalar Potential from a conservative force field – Work done by a force – Surface Integral – Volume integral – Theorems of Gauss, Stokes, and Green  
Fourier Series – Expansions of Periodic functions of period  $2\pi$  - Expansion of even and odd functions – half range series – Evaluation of Infinite Series using Fourier Series expansions – Fourier Transforms – Infinite Fourier Transform –  
Fourier Sine and Cosine transforms – Simple properties of Fourier Transforms – Convolution Theorem – Parseval's identity.

## **UNIT –V ALGEBRAIC STRUCTURES**

Groups – Subgroups, cyclic Groups and properties of cyclic groups, Lagrange's Theorem – Counting Principles –  
Normal subgroups, Quotient groups, Homomorphism, Automorphism, Cayley's theorem, Permutation groups – Rings –  
Some special classes of Rings – Integral domain, Homomorphism of rings – Ideal and Quotient rings – Prime ideal, Maximum Ideals – the field and quotients of an integral domain – Euclidean rings – Algebra of Linear transformation, Characteristic roots, matrices, Canonical forms, Triangular Forms – Problems of converting Linear Transformation to Matrices and vice-versa – Vector Space – Definition and examples – Linear dependence – Independence, Sub spaces and Dual spaces – Inner product spaces.



## UNIT-VI REAL ANALYSIS

Sets – Countable and Uncountable sets – Real Number system  $\mathbb{R}$  – Functions – Real Valued functions,  
Equivalence and Countability – Infremum and Supremum of a subset of  $\mathbb{R}$  – Bolzano-Weierstrass Theorem –  
Sequences of real numbers – Convergent and Divergent Sequences – Monotone Sequences – Cauchy Sequences –  
Limit Superior and Limit Inferior of a sequence – Sub Sequences – Infinite series – Alternating Series – Conditional convergence and Absolute convergence – Tests of Absolute convergence – Continuity and Uniform Continuity of a real valued function of a real variable – Limit of a function at a point – Continuity and Differentiability of real valued functions –  
Rolle's Theorem – Mean Value Theorems – Inverse function theorem, Taylor's Theorem with remainder forms – Power series expansion – Riemann Integrability – Sequences and Series of Functions.  
Metric spaces – Limits of a function at a point in metric spaces – functions continuous on a metric space – various reformulations of continuity of a function in a metric space - open sets – closed sets – discontinuous functions on the real line.

## UNIT VII COMPLEX ANALYSIS

Algebra of Complex Numbers – Function of Complex Variable – Mappings, Limits – Theorems on Limits, continuity, differentiability – Cauchy-Riemann Equations – Analytic Functions – Harmonic Function – Conformal mapping – Möbius Transformations – Elementary Transformation – Bilinear Transformations – Cross ratio – Fixed points of bilinear transformations – Special Bilinear transformations.  
Contours – Contour Integrals – Anti Derivatives – Cauchy-Goursat Theorem- Power Series – Complex Integration – Cauchy's theorem, Morera's theorem, Cauchy's Integral Formula – Liouville's Theorem – Maximum Modulus Principle – Schwarz's Lemma – Taylor's series – Laurent's series – Calculus of Residues – Residue Theorem – Evaluation of Integrals - Definite integrals of Trigonometric functions – Argument principle and Rouche's Theorem.



## UNIT VIII MECHANICS

Statics: Forces on a rigid body – Moment of a force – General motion of a rigid body – Equivalent system of forces – Parallel Forces – Forces along the sides of Triangle Couples. Resultant of several coplanar forces – Equation of line of action of the resultant – Equilibrium of rigid body under three Coplanar forces – Reduction of Coplanar forces into single force and couples – Laws of friction, angle of friction, Equilibrium of a body on a rough inclined plane acted on by several forces – Equilibrium of a uniform Homogeneous string – Catenary – Suspension bridge – Centre of Gravity of uniform rigid bodies. Dynamics: Velocity and Acceleration – Coplanar motion – Rectilinear motion under constant forces – Acceleration and retardation thrust on a plane – Motion along a Vertical line under gravity – Motion along an inclined plane – motion of connected particles – Newton's Laws of motion. Work, Energy and power – Work – Conservative field of force – Power –Rectilinear motion under varying force Simple Harmonic Motion (S.H.M) – S.H.M along a horizontal line – S.H.M along a Vertical line – Motion under gravity in a resisting medium. Path of a projectile – Particle projected on an inclined plane – Analysis of forces acting on particles and rigid bodies on static equilibrium, equivalent systems of forces, friction, centroids and moments of inertia – Elastic Medium, Impact – Impulsive force – Impact of sphere – Impact of two smooth spheres – Impact of two spheres of two smooth sphere on a plane – oblique impact of two smooth spheres. Circular motion – Conical Pendulum motion of a cyclist on circular path – Circular motion on a vertical plane – relative rest in revolving cone – simple pendulum – Central Orbits – Conic as Centered Orbit – Moment of inertia

## UNIT IX OPERATIONS RESEARCH

Linear Programming – Formulation – Graphical Solution – Simplex Method – Big –M method – Two phase method – Duality – Primal dual relation – dual simplex method – revised simplex method – Sensitivity analysis –



Transportation Problem – Assignment Problem – Queuing Theory – Basic Concepts – Steady State analysis of M/M/1

and M/M/Systems with infinite and finite capacities.

PERT-and CPM – Project network diagram – Critical path – PERT computations-Inventory Models- Basic

Concept –EOQ Models – uniform Demand rate infinite and finite protection rate with no shortage – Classical newspaper

boy problem with discrete demand – purchase inventory model with one price brake – Game theory – Two person Zero –

Sum game with saddle point – without saddle point – Dominance – Solving 2xn or mx2 game by graphical method –

Integer programming – Branch and bound method

## **UNIT—X STATISTICS/PROBABILITY**

Measures of central tendency – Measures of Dispersion – Moments – Skewness and Kurtosis – Correlation –

Rank Correlation – Regression – Regression line of x on y and y on x – Index Numbers – Consumer Price Index

numbers – Conversion of chain base Index Number into fixed base index numbers – Curve Fitting – Principle of Least

Squares – Fitting a straight line – Fitting a second degree parabola – Fitting of power curves – Theory of Attributes –

Attributes – Consistency of Data – Independence and Associate of data.

Theory of Probability – Sample Space – Axioms of Probability – Probability function – Laws of Addition –

Conditional Probability – Law of multiplication – Independent – Boole's Inequality – Bayes' Theorem – Random Variables

– Distribution function – Discrete and continuous random variables – Probability density functions – Mathematical

Expectation – Moment Generating Functions – Cumulates – Characteristic functions – Theoretical distributions –

Binomial, Poisson, Normal distributions – Properties and conditions of a normal curve – Test of significance of sample

and large samples – Z-test – Student's t-test – F-test – Chi square and contingency coefficient.